# Zigzag Octahedral Cluster Chains in $\mathrm{BaMo}_{6} \mathrm{O}_{\mathbf{1 0}}$ 

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#### Abstract

A novel ternary molybdenum oxide, $\mathrm{BaMo}_{6} \mathrm{O}_{10}$, was discovered and its crystal structure was determined from single-crystal X-ray diffraction data. $\mathrm{BaMo}_{6} \mathrm{O}_{10}$ crystallizes in the orthorhombic space group Pnma with $a=10.154(2), b=8.641(2), c=9.184(2) \AA, V=805.7(3) \AA^{3}, Z=4, R=0.0438, R_{\mathrm{w}}=$ 0.0401 for 652 independent reflections with $I>3.0 \sigma(I)$. The structure contains infinite zigzag molybdenum oxide chains built up from $M_{6} X_{12}$-type clusters, crosslinked to form channels where $\mathrm{Ba}^{2+}$ cations reside. Bond distance analysis results indicate that $\mathrm{BaMo}_{6} \mathrm{O}_{10}$ is perfectly bonded with all valence electrons of the Mo atoms in either Mo-Mo or Mo-O bonding states. o 1988 Academic Press, Inc.


## Introduction

There has been remarkable progress in the cluster chemistry of molybdenum oxides since the discovery of the milestone compound $\mathrm{NaMO}_{4} \mathrm{O}_{6}$ (I) about a decade ago. These reduced ternary oxides of molybdenum cover the range from discrete metal clusters (2), oligomers (3), and unidirectional condensed metal cluster chains ( 1 , 4-6), to condensed metal cluster chains running in two orthogonal directions (7).

Compounds with the composition $A_{x} \mathrm{Mo}_{4} \mathrm{O}_{6}$ ( $A=$ monovalent or divalent metal cations) are composed of infinite metal cluster chains based on trans-edgesharing $M_{6} X_{12}$-type clusters. The counter
cations occupy sites in channels formed by four metal cluster chains crosslinked by metal-oxygen bonds. The sodium ion in $\mathrm{NaMo}_{4} \mathrm{O}_{6}$, which crystallizes in a tetragonal space group, fully occupies the site at $\left(0,0, \frac{1}{2}\right)$. In $\mathrm{Ba}_{0.62} \mathrm{Mo}_{4} \mathrm{O}_{6}(5)$ and $\mathrm{Pb}_{0.77} \mathrm{Mo}_{4} \mathrm{O}_{6}$ (6), the channels can only be partially filled and the divalent cations are three-dimensionaliy ordered in the latice. The structure of $\mathrm{Ba}_{0.62} \mathrm{Mo}_{4} \mathrm{O}_{6}$ is a low-symmetry (orthorhombic) version of that of $\mathrm{NaMO}_{4} \mathrm{O}_{6}$ probably due to the electrostatic repulsion between the large divalent barium ions. Therefore, one expects a drastic structural modification of the $\mathrm{NaMo}_{4} \mathrm{O}_{6}$-type structure if the available sites in the channel are fully occupied by $\mathrm{Ba}^{2+}$. We report here the

TABLE I
Positional and Equivalent Isotropic Thermal
Parameters ${ }^{a}$ For $\mathrm{BaMo}_{6} \mathrm{O}_{10}$

| Atom | $x$ | $y$ | $z$ | $U_{\text {eq }}\left(\AA^{2} \times 10^{3}\right)$ |
| :---: | :---: | :---: | :---: | :---: |
| Ba | $0.3971(2)$ | 0.25 | 0.4959(2) | 7(1) |
| Mo1 | $0.0346(2)$ | 0.25 | $0.3827(2)$ | 6(1) |
| Mo2 | 0.9592(2) | 0.0844(2) | 0.6170(2) | 4(1) |
| Mo3 | $0.7222(2)$ | 0.25 | $0.6275(3)$ | 4(1) |
| Mo4 | 0.7862(2) | 0.0950(2) | $0.3865(2)$ | 4(1) |
| O1 | $0.9492(12)$ | $0.0880(13)$ | $0.2565(15)$ | 7(3) |
| O 2 | $0.6991(13)$ | -0.0828(14) | 0.2542(15) | 11(3) |
| O3 | $0.2060(18)$ | 0.25 | 0.2484(22) | 6(4) |
| 04 | 0.1426 (12) | $0.0920(14)$ | $0.5040(16)$ | 8(3) |
| 05 | $0.0433(18)$ | 0.25 | $0.7445(22)$ | 7(4) |
| 06 | $0.6319(11)$ | $0.0909(13)$ | 0.5091(16) | 6(3) |

${ }^{a}$ Equivalent isotropic $U$ is defined as one-third of the trace of the orthogonalized $U_{i j}$ tensor.
synthesis and crystal structure of the compound $\mathrm{BaMo}_{6} \mathrm{O}_{10}$ which contains zigzag metal oxide chains built up from $M_{6} X_{12}$-type clusters.

## Experimental

The discovery of $\mathrm{BaMo}_{6} \mathrm{O}_{10}$ was quite unintentional. During the investigation of molybdenum phosphates, a large number of new structures containing molybdenum in oxidation states less than +6 were discovered (see, e.g., (8)). Among these phosphates a few compounds contain silicon in the framework ( $\mathrm{Mo}_{3} \mathrm{P}_{5} \mathrm{SiO}_{19}$ : (9a); $\mathrm{MoP}_{3}$ $\left.\mathrm{SiO}_{11}:(9 b)\right)$. The silicon contents were from the fused silica tubes as reaction containers. Attempts were planned for the preparation of early transition metal silicates. A reaction mixture containing $\mathrm{BaMoO}_{4}, \mathrm{MoO}_{3}$, and Mo (mole ratio $1: 1: 1$ ) was sealed in a fused silica tube and the reaction conducted at $1200^{\circ} \mathrm{C}$ for several days. Upon opening the devitrified and shrunk silica tube, some black, chunky crystals were found in the bulk product. The structural determination of one of these chunks indicated that the composition was $\mathrm{BaMo}_{6} \mathrm{O}_{10}$. A black chunk having the dimensions $0.12 \times 0.08 \times 0.06$ mm was selected for indexing and intensity data collection. The compound crystallizes
in the orthorhombic space group Pnma (No. 62) with one Ba , two Mo, and two O at 4 c special positions, and two Mo and four $O$ at general positions. The multiplicity of the Ba atom was allowed to refine but did not deviate significantly from full occupancy. Crystal data for $\mathrm{BaMo}_{6} \mathrm{O}_{10}$ : space group Pnma, $a=10.154(2), b=8.641(2), c=$ 9.184(2) $\AA, V=805.7(3) \AA^{3}, Z=4, D_{c}=$ $7.20 \mathrm{~g} / \mathrm{cm}^{3}$. A total of 762 reflections were obtained of which 652 had $I>3.0 \sigma(I)(86 \%$ observed) giving a data : parameter ratio of 10.9:1 and $R=0.0438, R_{w}=0.0401$, and $\mathrm{GOF}=3.64$. For MoK $\alpha$ radiation, $\mu=$ $136.67 \mathrm{~cm}^{-1}$ and an empirical absorption correction was applied. The Ba and Mo atoms were refined anisotropically and the O atoms were refined isotropically. Final positional and thermal parameters are collected in Table I. Selected bond distances are given Table II.

## Description and Discussion of the Structure

A view of the structure is shown in Fig. 1 , which depicts the infinite $\mathrm{Mo}_{6} \mathrm{O}_{10}$ chains

TABLE II
Selected Interatomic Distances (Å) FOR $\mathrm{BaMO}_{6} \mathrm{O}_{10}$

| Ba-O1 | $2.76(1)(2 \times)$ | Mo1-O1 | $2.01(1)(2 \times)$ |
| :--- | :--- | :--- | :--- |
| Ba-O2 | $2.89(1)(2 \times)$ | Mo1-O3 | $2.14(1)$ |
| Ba-O3 | $2.99(2)$ | Mo1-O4 | $2.08(1)(2 \times)$ |
| Ba-O4 | $2.92(1)(2 \times)$ | Mo2-O1 | $2.11(1)$ |
| Ba-O5 | $2.81(1)$ | Mo2-O2 | $2.04(1)$ |
| Ba-O6 | $2.76(1)(2 \times)$ | Mo2-O4 | $2.13(1)(2 \times)$ |
| Ba-O6 | $2.96(1)(2 \times)$ | Mo2-O5 | $2.04(1)$ |
| Mo1-Mo2 | $2.695(3)(2 \times)$ | Mo3-O2 | $2.02(1)(2 \times)$ |
| Mo1-Mo2 | $2.890(3)(2 \times)$ | Mo3-O5 | $2.16(1)$ |
| Mo1-Mo4 | $2.856(3)(2 \times)$ | Mo3-O6 | $1.98(1)(2 \times)$ |
| Mo2-Mo2 | $2.730(3)$ | Mo4-O1 | $2.04(1)$ |
| Mo2-Mo2 | $2.861(3)$ | Mo4-O2 | $2.15(1)$ |
| Mo2-Mo3 | $2.802(3)$ | Mo4-O3 | $2.00(1)$ |
| Mo2-Mo4 | $2.753(2)$ | Mo4-O4 | $2.04(1)$ |
| Mo2-Mo4 | $3.015(3)$ | Mo4-O6 | $1.93(1)$ |
| Mo3-Mo4 | $2.668(3)(2 \times)$ |  |  |
| Mo4-Mo4 | $2.679(3)$ |  |  |



Fig. 1. A three-dimensional view down the $b$ axis of $\mathrm{BaMo}_{6} \mathrm{O}_{10}$. The $\mathrm{Ba}, \mathrm{Mo}$, and O atoms are represented by large cross-hatched circles, small dotted circles, and medium open circles, respectively. Heavy lines are Mo-Mo bond and thin lines are Mo-O bonds.
running parallel to the $b$-axis. Four infinite chains are interlinked through Mo-O-Mo bonds to form channcls where the $\mathrm{Ba}^{2+}$ ions are located. A segment of one of the chains
is provided in Fig. 2, which reveals that the chain consists of $M_{6} X_{12}$-type clusters linked on opposite edges in a zigzag way. The molybdenum atoms are found to have different


FIG. 2. A section of a zigzag octahedral cluster chain of $\mathrm{BaMo}_{6} \mathrm{O}_{10}$ as viewed perpendicular to the chain axis.


Fig. 3. The coordination environment of the $\mathrm{Ba}^{2+}$ ion in $\mathrm{BaMo}_{6} \mathrm{O}_{10}$. The $\mathrm{Ba}, \mathrm{Mo}$, and O atoms are represented by large, small, and medium open circles, respectively.
coordination numbers: Mo1 (5 O + 6 Mo ), $\mathrm{Mo} 2(5 \mathrm{O}+7 \mathrm{Mo}), \mathrm{Mo} 3(5 \mathrm{O}+4 \mathrm{Mo})$, and Mo4 ( $5 \mathrm{O}+5 \mathrm{Mo}$ ). For each cluster unit there are 12 intracluster bonds and 5 intercluster bonds, with distances ranging from 2.668 to $3.015 \AA$. The apex Mo atoms (Mo1, Mo3) lie in mirror planes perpendicular to the $b$-axis at $y=\frac{1}{4}$. The Mo-Mo bond distances within a cluster unit, Mo1-Mo4 (2.856), Mo1-Mo2 (2.695), Mo2-Mo2 (2.861), Mo4-Mo4 (2.679), Mo2-Mo4 (2.753), Mo2-Mo3 (2.802), and Mo3-Mo4 ( $2.668 \AA$ ), result in an average distance of $2.759 \AA$, which is only $0.032 \AA$ longer than the distance between nearest neighbors in bcc molybdenum metal. There are three different intercluster Mo-Mo bond lengths of $2.890 \AA$ (mo1-Mo2), $2.727 \AA$ (Mo2-Mo2), and $3.015 \AA$ (Mo2-Mo4). All Mo atoms are each bonded to five $O$ atoms. The Mo-O bond distances range from 1.930 to $2.163 \AA$,
with the shortest of these involving the oxygen atom bridging only one octahedron edge. The oxygen atoms $\mathrm{O} 2, \mathrm{O} 3$, and O 5 lie above octahedra edges but coordinate neighboring cluster chains in corner positions ( $\mathrm{O}^{\mathrm{i}-\mathrm{a}}$ or $\mathrm{O}^{\mathrm{ai}}$ ). Oxygen 1 and 4 are each shared between cluster units within the chains ( $\mathrm{O}^{\mathrm{i}-\mathrm{i}}$ ). Oxygen 6 bridges only one octahedron edge ( $\mathrm{O}^{\mathrm{i}}$ ). Therefore, both intraand intercluster sharing of atoms can be described in the connectivity formula $\mathrm{Ba}^{2+}\left[\mathrm{Mo}_{6}\left(\mathrm{O}_{2}{ }_{2} \mathrm{O}^{\mathrm{i}-\mathrm{i}}{ }_{4 / 2} \mathrm{O}^{\mathrm{i}-\mathrm{a}}{ }_{6 / 2}\right) \mathrm{O}^{\text {a-i }}{ }_{6 / 2}\right]^{2-}$. Of special note is the peculiar geometry around O4 which is bonded to four Mo atoms within the chains. Figure 3 shows the coordination environment of the $\mathrm{Ba}^{2+}$ ion in Ba $\mathrm{Mo}_{6} \mathrm{O}_{10}$. The $\mathrm{Ba}^{2+}$ ion is surrounded by 12 oxygen atoms at distances of 2.757 to 2.986 $\AA$. The $\mathrm{Ba}-\mathrm{O}$ distances arc a little shorter than the calculated $\mathrm{Ba}-\mathrm{O}$ distance ( $2.99 \AA$ ) based on $\mathrm{Ba}^{2+}(1.61 \AA, \mathrm{CN}=12)$ and $\mathrm{O}^{2-}$ ( $1.38 \AA, \mathrm{CN}=4$ ) (10) and accordingly the $\mathrm{Ba}^{2+}$ ion is tightly bonded to the oxygen atoms and does not exhibit large thermal parameters.

The average valence of Mo in $\mathrm{BaMo}_{6} \mathrm{O}_{10}$ is +3 . An assessment of the valence of the individual Mo atoms using the bond-length bond-strength formula (11) for the Mo-O bond $\left[s=\left(d_{\mathrm{MO}-0} / 1.882\right)^{-6.0}\right]$ yields the following results: Mo1, +2.94 ; Mo2, +2.66 ; Mo3, +3.22; Mo4, +3.24. The summation of the assessed valences over the Mo atoms of the cluster repeat unit is equal to 17.96 , which is in excellent agreement with the value of 18 based on the stoichiometry. The bond orders for the Mo-Mo bonds can be calculated by using the Pauling bond order (PBO) equation $d_{n}=d_{1}-0.6 \log n(12)$, where $d_{n}$ and $d_{1}$ are the bond distances for bonds of order $n$ and 1 , respectively, and $n$ is the bond order. The sum of the number of electrons devoted to Mo-O bonding and the number of electrons devoted to Mo-Mo bonding should be equal to the periodic group number if all valence electrons of the metal atom are involved in bonding. A
calculation using the bond-length bondstrength formula and the PBO equation $\left(d_{1}(\mathrm{Mo}-\mathrm{Mo})=2.614 \AA\right)$ for the Mo atoms in $\mathrm{BaMo}_{6} \mathrm{O}_{10}$ gives: $\mathrm{Mo1}, 5.89$; Mo2, 6.06; Mo3, 5.82; Mo4, 6.01. The sum over individual Mo-Mo bonds of the cluster repeat unit using the PBO equation yields 8.97. The metal-centered electron (MCE) available for metal-metal bonding is $17.94(=2$ $\times 8.97$ ). The number of antibonding electrons is one-half of the difference between the MCE derived from PBO sums and the MCE derived from the formula of the compound (13). Thus, within the limits of error $\mathrm{BaMo}_{6} \mathrm{O}_{10}$ has no electrons in antibonding states. These results indicate that Ba $\mathrm{Mo}_{6} \mathrm{O}_{10}$ is perfectly bonded with all valence electrons of the Mo atoms in either Mo-Mo or Mo-O bonding states.

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